TCAD Parameters for 4H-SiC: A Review

Jürgen Burin,¹ Philipp Gaggl,¹ Simon Waid,¹ Andreas Gsponer,¹ and Thomas Bergauer¹ Institute of High Energy Physics, Austrian Academy of Sciences, Nikolsdorfer Gasse 18, 1050 Wien

(*e-mail: juergen.burin@oeaw.ac.at)

(Dated: 16 October 2024)

In this paper we review the models and their parameters to describe the relative permittivity, bandgap, impact ionization, mobility, charge carrier recombination/effective masses and incomplete dopant ionization of 4H silicon carbide in computer simulations. We aim to lower the entrance barrier for newcomers and provide a critical evaluation of the status quo to identify shortcomings and guide future research. The review reveals a rich set of often diverging values in literature based on a variety of calculation and measurement methods. Although research for all the selected parameters is still active, we show that sometimes old values or those determined for other kinds of silicon carbide are commonly used.

Keywords: 4H-SiC, TCAD simulations, simulation parameters, silicon carbide

CONTENTS

| I. Incomplete Ionization | 3 |
|--------------------------|----|
| A. Theory | 3 |
| B. Results | 6 |
| C. Discussion | 11 |
| References | 17 |

I. INCOMPLETE IONIZATION

It is indispensable to add a doping to a semiconductor, i.e., to introduce impurity atoms, in order to create sophisticated electronic devices. These so-called dopants add energy levels near to the conduction (n-type doping) resp. valence band (p-type doping) such that free charge carrier can be injected at moderate temperatures. In this fashion the electrical characteristics of the material can be altered. Partial overviews on available doping elements and their respective activation energies in 4H-SiC are available^{1–21}. Uncommon elements were also investigated. Ab initio calculations by Miyata, Higashiguchi, and Hayafuji²² identified Arsenic²³, Gallium²⁴ or Antimony as, energy level wise, fitting. Group IV elements were investigated by Krieger *et al.*²⁵, Feng and Zhao⁵, Huang *et al.*²⁶ focused on Tantalum and Chromium and Dalibor and Schulz³, Dalibor *et al.*²⁷ on Vanadium. Additional factors such as the activation rates²⁸ or the impact of hydrogen²⁹ might, however, prevent the deployment of these dopants.

Due to the wide bandgap of 4H-SiC the respective dopant activation energies are large such that the often used assumption of full ionization is not applicable. Quite the opposite: incomplete ionization has to be carefully considered to correctly predict the amount of free charge carriers and, thus, achieve a realistic conductivity^{30,31}.

In this section we will, thus, review measurements, models and TCAD parameters used to described the amount of ionized dopants depending on temperature and doping concentration. We focus on the four most common doping species in 4H-SiC^{32–34}: Aluminum (analysis by Darmody and Goldsman³⁵) and Boron for p-type resp. Nitrogen and Phosphorous for n-type doping. We limit ourselves to simple model, e.g., a single energy level per lattice site (cubic or hexagonal). Depending on various parameters, e.g., binding type and location^{36–39} or whether the impurity is located in a non-neutral regions or not³¹, rather elaborate descriptions would be necessary to account otherwise⁴⁰.

A. Theory

A good overview on the physical descriptions of incomplete ionization is provided by³². In brief, the amount of ionized dopants can be modeled by the Fermi-Dirac distribution^{12,41–44}, also

known as steady-state Gibbs distribution³¹, as

$$N_{\rm D}^{+} = \frac{N_{\rm D}}{1 + g_{\rm D} \exp\left(\frac{E_{\rm F,n} - E_{\rm D}}{k_{\rm B}T}\right)}$$

$$N_{\rm A}^{-} = \frac{N_{\rm A}}{1 + g_{\rm A} \exp\left(\frac{E_{\rm A} - E_{\rm F,p}}{k_{\rm B}T}\right)}$$
(1)

where N_A resp. N_D are the active acceptor resp. donor concentrations, E_A resp. E_D the acceptor resp. donor energy levels, $E_{F,n}$ resp. $E_{F,p}$ the electron resp. hole Fermi level and g_D resp. g_A the degeneracy factors. The latter denote the degeneracy of the energy levels⁴⁵, whereat in the literature commonly the values $g_A = 4$ (spin up and spin down plus two valence bands) and $g_D = 2$ (spin up and down)^{30,46} are used. There are, however, exception: Troffer⁴⁷ used $g_D = 6$,Scaburri³², Laube *et al.*⁴⁸ a spin degeneracy of $g_D = 4$ for Phosphorous, Balachandran, Chow, and Agarwal⁴⁹, Nawaz⁵⁰ $g_A = g_D = 3$,Persson and Lindefelt⁵¹ $g_A = 2$, Lv *et al.*⁵² $g_A = g_D = 2$ and Pernot *et al.*⁵³ $g_k = 6$ resp. $g_h = 2$ for the cubic resp. hexagonal site of Nitrogen. There were also efforts to introduce a temperature dependency as $G_A(T)$ and $G_D(T)^{17,32,47,54-57}$, whereat the description by Lophitis *et al.*⁵⁸ (equ. (11)) deviates significantly.

If solely Boltzmann statistics are considered Eq. (1) can be simplified to^{20,32,59–61}

$$N_{\rm D}^{+} = \frac{N_{\rm D}}{1 + g_{\rm D} \frac{n}{N_{\rm C}} \exp\left(\frac{\Delta E_{\rm D}}{k_{\rm B}T}\right)}, \qquad n = N_{\rm C} \exp\left(\frac{E_{\rm F,n} - E_{\rm C}}{k_{\rm B}T}\right)$$

$$N_{\rm A}^{-} = \frac{N_{\rm A}}{1 + g_{\rm A} \frac{p}{N_{\rm V}} \exp\left(\frac{\Delta E_{\rm A}}{k_{\rm B}T}\right)}, \qquad p = N_{\rm V} \exp\left(\frac{E_{\rm V} - E_{\rm F,p}}{k_{\rm B}T}\right)$$
(2)

with $N_{\rm C}$ resp. $N_{\rm V}$ the effective density of states in the conduction resp. valence band (see ??) and $\Delta E_{\rm D} = E_{\rm C} - E_{\rm D}$ resp. $\Delta E_{\rm A} = E_{\rm A} - E_{\rm V}$ the ionization energies of donors and acceptors relative to the conduction ($E_{\rm C}$) and valence band ($E_{\rm V}$). This representation is often preferred in TCAD simulation tools, which commonly operate on charge carrier concentrations.

For completeness we want to highlight that using the neutrality equation³²

$$N_{\rm D}^+(E_{\rm F}) + p(E_{\rm F}) = N_{\rm A}^-(E_{\rm F}) + n(E_{\rm F})$$
(3)

it is possible to even get rid of the carrier concentration. If we assume a highly donor doped material ($p(E_{\rm F})$ can be neglected) and no compensation ($N_{\rm A}^-(E_{\rm F}) = 0$) Eq. (3) results, by inserting Eq. (2) for $N_{\rm D}^+$, in a quadratic equation for *n* which can be solved to^{34,62–67}

$$N_{\rm D}^{+} = N_{\rm D} \frac{-1 + \sqrt{1 + 4g_{\rm D} \frac{N_{\rm D}}{N_{\rm C}} \exp\left(\frac{\Delta E_{\rm D}}{k_{\rm B}T}\right)}}{2g_{\rm D} \frac{N_{\rm D}}{N_{\rm C}} \exp\left(\frac{\Delta E_{\rm D}}{k_{\rm B}T}\right)}$$

We have to highlight that the solution of the quadratic expression for n by Scaburri³² is incorrect, which makes it impossible to retrace the presented, correct, equation for $N_{\rm D}^+$. Accordingly an expression for $N_{\rm A}^-$ can be achieved.

The ionization energies also depend on the doping concentration. This can be explained by the changing potential energy of the charge carriers when they are closer to the ionized atoms, effectively shielding them⁶⁸. To model the decrease in the ionization energy the Pearson-Bardeen⁶⁸ expression

$$\Delta E(N) = \Delta E_0 - \alpha N^{1/3} \tag{4}$$

is used.

The literature is inconsistent on what dopants should be included into the overall doping concentration N in Eq. (4). Some authors include both donors and acceptors $N_A + N_D^{59,60}$, others only the respective donor concentration (N_A or N_D)^{54,69–73}, while a third group just uses the ionized ones⁷⁴. Kajikawa⁷⁵ even argues that the compensating dopants, i.e., donors for the acceptor levels and vice versa, have the bigger impact and should be used instead of the overall donor and acceptor concentrations. There have also been proposals to include the compensating dopants into the factor $\alpha^{32,76}$. Finally, a completely different approach focuses on the degree of compensation depicted by a screening of free charge carriers^{32,77}, which introduces an additional temperature dependency.

An alternative approach to the Pearson-Bardeen expression in Eq. (4) is given by Altermatt, Schenk, and Heiser⁷⁸, Altermatt *et al.*⁷⁹, who used the logistic equation

$$\Delta E(N) = \frac{\Delta E_0}{1 + (N/N_{\rm E})^c} \tag{5}$$

to model the decrease in ionization energy, with $N_{\rm E}$ a reference concentration where the ionization energy is half its original value ΔE_0 . Darmody and Goldsman³⁵ argue that with Eq. (4) it is possible to shift the dopant level into the conduction/valence band and thus ionize all dopants immediately, which is neither physically reasonable nor possible with Eq. (5). Despite these arguments, the described approach has not yet found its way into the major simulation tools.

Dopants have differing ionization energies depending on whether they are located in a hexago-

nal or a cubic lattice site⁸⁰ (see ??). Consequently Eq. (2) has to be adapted to^{23,60}

$$N_{\rm D}^{+} = \frac{\frac{1}{2}N_{\rm D}}{1 + g_{\rm D}\frac{p}{N_{\rm C}}\left(\frac{\Delta E_{\rm Dh}}{k_{\rm B}T}\right)} + \frac{\frac{1}{2}N_{\rm D}}{1 + g_{\rm D}\frac{p}{N_{\rm C}}\left(\frac{\Delta E_{\rm Dc}}{k_{\rm B}T}\right)}$$
$$N_{\rm A}^{-} = \frac{\frac{1}{2}N_{\rm A}}{1 + g_{\rm A}\frac{p}{N_{\rm V}}\left(\frac{\Delta E_{\rm Ah}}{k_{\rm B}T}\right)} + \frac{\frac{1}{2}N_{\rm A}}{1 + g_{\rm A}\frac{p}{N_{\rm V}}\left(\frac{\Delta E_{\rm Ac}}{k_{\rm B}T}\right)}$$

with E_{Dc} and E_{Dh} the cubic resp. hexagonal ionization energies for donors and E_{Ac} and E_{Ah} for acceptors. The factors 1/2 denote that both lattice sites are equally probable⁶¹. In TCAD simulations it is often the case that these separate values are merged to an effective energy level, ending up once again in a description as shown in Eq. (2)^{13,59,65,81,82}. The effects of such simplifications have been investigated by Lades⁸³, Ayalew *et al.*⁸⁴.

For more accurate approximation of dynamic processes around the dopant, i.e., (de)trapping of charge carriers, the electron and hole cross sections are crucial (see ??). There are multiple description available in literature, which differ in their temperature scaling⁸⁵. The multi-phonon capture model is independent of temperature^{86–88} while the cascade capture model is proportional to $T^{-289-91}$. Kaindl *et al.*⁹² argue that the latter delivers a better fit. A scaling with T^{-3} was used by Kuznetsov and Zubrilov⁹³. Note that we discovered large discrepancies between the single tools regarding which models are supported.

B. Results

The most commonly method to determine the ionization energy of dopants in literature is to fit the neutrality equation, i.e., for p-type doping

$$p + N_{\rm K} = \frac{N_{\rm A}}{1 + \frac{g_{\rm A}p}{N_{\rm V}} \exp\left(\frac{\Delta E_{\rm A}}{k_{\rm B}T}\right)} \ .$$

to Hall measurements, e.g., conductivity or charge carrier concentration, for varying temperature^{24,38,46,47,53,56,57,66,69,71,73,75,91,94–122}. The compensation doping density $N_{\rm K}$ is only required for fitting purposes, such that we solely use $N_{\rm A}$ as the doping density to present our results. Due to the anisotropy of the Hall effect it is possible to achieve direction dependent ionization energies this way⁵⁶. Other approaches based on Hall measurements include the fitting to the activation ratio¹²³ or free carrier concentration spectroscopy (FCCS)^{54,70,124}. Further used electrical measurements are (thermal)^{125–128} admittance spectroscopy (AS)^{24,47,56,73,91,92,102,129}, electron spin resonance (ESR) measurement¹³⁰, deep level transient spectroscopy (DLTS)^{56,93,131,132} and minority carrier transient spectroscopy $(MCTS)^{131}$, which are often combined with Hall measurements for more accurate results. Troffer⁴⁷ notes that DLTS is more sensitive but admittance spectroscopy allows to depict time constants below 1 μ s.

These electrical methods are complemented by optical ones, e.g., (fourier transform infrared) photothermal ionization spectroscopy (PTIS)¹³³, donor-acceptor pair (DAP) luminescence^{80,134–136}, free to acceptor (FTA) spectroscopy⁸⁰, infrared absorption (IA)⁹⁸, photoluminescence (PL)^{102,137–140}, time-resolved spectroscopy (TRS)¹³⁷ or delay measurements (DM)¹³⁷. In these cases electrons are empowered and the resulting photon emission is recorded. The latter can be cause by transitions among traps or between traps and the conduction/valence band⁵⁶. Note that different methods lead to slightly deviating results, even when applied to the same device⁹⁸. Also possible are calculations, e.g., Faulkner model (FM) calculations¹⁴¹, density functional theory (DFT)^{22,142}, effective mass approximation (EMA)¹⁴³, first principles calculations (FPC)^{26,29,39} or *ab initio* supercell calculations (AISC)¹⁴⁴. Finally, some authors define a value range based on measurements in literature^{34,61,83}, calculate an average values¹⁴⁵ or fit to existing data^{35,60,146}.

In the sequel we are going to present the ionization energies ΔE_D resp. ΔE_A found in literature with their respective doping concentration. In order to draw the measurements we dropped uncertainties and replaced the sometimes stated exciton energy E_x with 20 meV (see ??). We had to discard results where the samples were solely described as "high purity" or "unintentional doping"^{96,138–140} and Laube *et al.*⁴⁸, which was superseded by a publication of the same authors. We mark results for the hexagonal lattice site by a trailing "h" and result for the cubic one by a trailing "c". The latter is often also denoted by the letter "k", which, most probably, corresponds to the german word "kubisch" for cubic. In fact, some of the literature is written in german^{47,56}, making it hard to retrace the results for the international community.

For Aluminum (see Fig. 1) many measurements and model fittings have been proposed. The values are equally distributed across the last three decades, meaning that the improvements in material quality did not result in significant changes. The model proposed by Achatz *et al.*⁷² uses the critical aluminum concentration for the doping-induced metal-insulator transition to set $\Delta E_{\rm A} = 0$ and then fit the parameters. This is in contrast to the logistic equation in Eq. (5) used by Darmody and Goldsman³⁵, where a much slower decrease of $\Delta E_{\rm A}$ below 100 meV can be observed.

For low-doped and compensated devices a second energy level is required to properly describe the measurements⁷¹. The origin of this deep level is still discussed in literature. Matsuura *et al.*^{54,}



FIG. 1. Aluminum ionization energy. Marks refer to measurements and lines to fittings. The letter 'd' after the reference indicates a deep level whose origin is still discussed (see text). Colors are used solely to increase the readability.

¹²⁴ were not able to provide any explanation, Weiße *et al.*⁷³ suspect excited states of the aluminum ground state and Pernot, Contreras, and Camassel⁷¹, Smith, Evwaraye, and Mitchel¹²⁶ describe them as the cubic lattice site. In fact, Smith, Evwaraye, and Mitchel¹²⁶ states that for higher concentration only the hexagonal site is measured. Nevertheless, in our plots we show the data as presented by the original authors, with the exceptions of the ones by Saks *et al.*¹¹⁵, which Pernot, Contreras, and Camassel⁷¹ pointed out to denote the cubic lattice site.

Aluminum is the single dopant where a fitting using the logistic approximation (see Eq. (5)) was used. Darmody and Goldsman³⁵ achieved $\Delta E_0 = 214.86 \text{ meV}, N_E = 8.12 \times 10^{19} \text{ cm}^{-3}$ and c = 0.632.

The available measurements for Boron (see Fig. 2) are very few and date back to the last millennium. We suspect the main cause in the deep D-center^{35,39,47} that comes with a Boron doping. It introduces an energy level in a range of $495-630 \text{ meV}^{47,80,91,93,131,134}$, which results



FIG. 2. Boron ionization energy. Marks refer to measurements and lines to fittings. Colors are used solely to increase the readability.

in a very effective recombination center. In some publications and also in some simulation tools the D-center level is used as the actual Boron one^{9,80,134,140,147–150}. Since only a single fitting according to Eq. (4) is available for Boron we used all the available data to generate an additional one (t.w.).

For the n-type donor Nitrogen (shown in Fig. 3) almost all publications distinguish between cubic and hexagonal site. However, there is also a big spread in the data, especially towards higher doping concentrations. The results suggest that the ionization energy does not decrease (especially for the cubic lattice site) even as the solubility limit (1×10^{19} cm³ for annealing at 1700 K up to 3×10^{20} cm³ for annealing at 2500 K^{16,136,150–152}) is approached.

For Nitrogen only fittings according to Eq. (4) are available. Kagamihara *et al.*⁷⁰ provided a fitting for both hexagonal and cubic lattice site, which were combined by Hatakeyama, Fukuda, and Okumura⁶⁰ to an effective ionization energy model. The remaining fittings also represent effective levels but are surprisingly low. In the case of Buono⁵⁹ this can be explained by the the selection of ΔE_0 , which was picked as the effective value of 65 meV determined by Bakowski, Gustafsson, and Lindefelt⁸¹ based on the values from Götz *et al.*⁹⁸. The latter, as can be seen in the figure, were, however, determined for a doping of 1×10^{17} cm⁻³ resp. 1×10^{18} cm⁻³.

Compared to Nitrogen a lot less measurements are available for Phosphorous (see Fig. 4), all roughly two decades old. Again, hexagonal and cubic lattice site are always distinguished, but the results especially for the latter largely deviate. Due to the lack of fittings according to Eq. (4) we used the available data to generate very crude fittings. Even as the solubility limit (6×10^{18} cm³ for annealing at 1700 K up to 2×10^{20} cm³ for annealing at 2500 K^{16,136,150–152}) is reached high



FIG. 3. Nitrogen ionization energy. Marks refer to measurements and lines to fittings. Colors are used solely to increase the readability.



FIG. 4. Phosphorous ionization energy. Marks refer to measurements and lines to fittings. Colors are used solely to increase the readability.

ionization energies for the cubic lattice site are observable.

The parameters for the Pearson-Bardeen model (see Eq. (4)) fittings, which were shown in Figs. 1 to 4, are summarized in Table I. We also added our own fitting parameters (t.w.). To take the described inconsistency for N in Eq. (4) into account column N denotes either the total doping (tot), the n- resp. p-type doping (dop), the compensation (comp) or fitting (fit). For the figures we used uniformly the specific doping concentration N_A resp. N_D (x-axis).

Cross-sections with varying temperature were heavily investigated at the end of the last century (see Table II). The column σ denotes the cross section with the charge carrier in the energetically closer band (conduction or valence) because the interaction with the other band is significantly lower^{47,92}.

Finally we also investigated single energy values used in overviews or in TCAD simulations (see Fig. 5). We do not show fundamental values here as these are always linked to a specific doping concentration. For Aluminum many publications use a value that corresponds to the deeper (cubic site?) energy level. Also for Boron some values refer to the deep D-center. Altogether, a wide range of values is used, especially for Nitrogen, where again hexagonal and cubic sites are almost always distinguished. We want to highlight that for the Boron ionization energy of 293 meV^{31,58,153} no direct connection to any fundamental investigation could be inferred.

In some publications the dopant is not clearly specified. Instead only the acceptor and donor energy level are provided (see Fig. 6). While the acceptor values clearly correspond to Aluminum the n-type values could belong to both Nitrogen and Phosphorous.

C. Discussion

In contrast to other properties that have been investigated within this review, there exist a lot of fundamental studies and measurements for incomplete ionization. Nevertheless, the results acquired over the last decades deviate sometimes significantly, making it impossible to distill them to common values. This is, by the way, not caused by less mature samples in the past. Even by limiting our analysis to the last two decades we did reveal a large spread in measurement results. The situation is worsened by the fact that values for hexagonal and cubic lattice sites are often used without appropriate notation. In this fashion significant errors can be introduced, especially for Boron where the deep levels is approximately twice the shallow one.

Overall, almost all publications utilize values determined from 4H-SiC measurements. Only

| | | | | 100 | [Heni13] ¹⁷⁷ [Gerh11] ¹⁸⁴ [c] [Bali06] ¹⁶⁵ [Gao01] ¹⁵⁹ | | |
|---------------------|-----------------------------------------------------------------------------------------------------------------------------------------------|-----------------|------------------------------------------------------|------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------|------------|------------------------------------------------------------|
| | | | 150 | 92 | [Zhu08] ²¹ [c] [Zett02] ²⁰ [c] | | |
| | | 700 | [Gao01] ¹⁵⁹ | 91.8 | [Buon12] ⁵⁹ [c] [Wang99] ¹⁶² [c] [Pers99a] ¹⁸³ [c] [Greu97] ¹⁴⁸ [c] [Bako97] ⁸¹ [c] | | |
| | | 650 | [Levi01] ¹¹ | 91 | [Bhat05] ⁸² [c] | | |
| | | | [Ioff23] ¹⁴⁷ | 90 | [Pank14] ¹⁶ [c] | | [Kimo19] ¹⁵² [c] |
| | | 647 | [Fan14] ¹⁴⁹ [Grau071 ¹⁴⁸ | 90 ± 5 | [Alba10] ³⁴ [c] [Ayal05] ⁸⁴ [c] [Ayal04] ⁶¹ [c] | 120 | [Nipo18] ³³ [c] [Kimo14a] ¹⁶⁴ [c] |
| 270 | [Pank14] ¹⁶ [Heni13] ¹⁷⁷ | | [Made91] ¹⁵⁰ | 90 ± 10 | [Schr06] ¹⁶⁸ [c] [Lade00] ⁸³ [c] | 120 | [Scab11a] ³² [c] |
| 265 | [Tiwa19a] ¹⁷³ [Tiwa19] ¹⁷⁴ | | | 81 | [Bhat05] ⁸² [e] [Mick98] ¹⁸² [c] | | [Scab11] ⁷⁷ [c] |
| 203 | [Loph18] ⁵⁸ [Dona18] ³¹ [Arva17] ¹⁵³ | 628 ± 1 +Ex | [Deva97] ¹³⁴ | 80 | [Sull08] ¹⁷⁹ | 102 | [Dona18] ³¹ [c] |
| | | | | 77 | [Lutz18] ¹³ [Lutz11] ¹² | | [Zhu08] ²¹ [c] |
| 230 | [Huan22b] ¹⁷² [Huan22a] ²⁶ | 390 | [Pank14] ¹⁶ [Heni13] ¹⁷⁷ | 71 | [Loph18] ⁵⁸ [Arva17] ¹⁵³ | 93 | [Zett02] ²⁰ [c] |
| 220 ± 20 | [Ayal05] ⁸⁴ [Ayal04] ⁶¹ | | | 70.9 | [Tiwa19a] ¹⁷³ [Tiwa19] ¹⁷⁴ | | [Handoo] [C] |
| 220 | [Lu21] ¹⁴² [Trew02] ¹⁷¹ | 340 | [Torr22] ³⁹ [c] | 70 | [Megh18] ¹⁵⁵ [Dona18] ³¹ [h] [Ayal05] ⁸⁴ [e] [Ayal04] ⁶¹ [e] | 90 ± 5 | [Alba10] ³⁴ [c] |
| 210 | [Nipo18] ³³ [c] [Lutz18] ¹³ | | [Alba10] ³⁴ | 66 | [Ioff23] ¹⁴⁷ [h] [Fan14] ¹⁴⁹ [h] [Izzo08] ¹⁸⁷ [h] [Made91] ¹⁵⁰ [h] | 80 | [Wije11] ¹⁵⁶ |
| 210 | [Usma12] ¹⁶⁹ [Lutz11] ¹² [Buon10] ¹⁷⁰ | 330 ± 30 | [Ayal05]84 | | | 80 | [Neud06] ¹⁵ [Neud01] ¹⁴ |
| 210 ± 20 | (+)) 10130 (0 1 0/2168 (T 1 0/283) | | [Ayal04] ⁶¹ | 65 | [Rakh20] ¹⁷⁸ [Joha19] ¹⁷⁰ [Usma12] ¹⁵⁹ [Buon10] ¹⁷⁰ [Wang99] ¹⁶² [e] [Bako97] ⁸¹ [e] | | |
| 210 ± 20 | [Alba10] [Schlob] [Ladeoo] | | [Torr22] ³⁹ [h] [Lutz18] ¹³ | | | 76 | [Son06] ¹⁴⁴ [c] |
| 201.3 | [Tian20] ¹⁶⁷ [Janz08] ¹⁶³ [c] | 320 | [Lutz11] ¹² | 61.4 | [Pern00] ³⁵ [h] [Tian20] ¹⁶⁷ [Janz08] ¹⁶³ [h] | (0.7 | [Scab11a] ³² [h] |
| 201 | [Kimo19] ¹⁵² [c] [Kimo14a] ¹⁶⁴ [c] | | [Saks01] ¹¹⁵ | 61.4+0.5 | [Ivan03a] ¹⁴¹ [h] | 60.7 | [Scab11] ⁷⁷ [h] |
| | | 320 ± 20 | [Schr06] ¹⁶⁸ | 61 | [Yang19] ¹⁸⁶ [Kimo19] ¹⁵² [h] [Kimo14a] ¹⁶⁴ [h] | | [Kimo19] ¹⁵² [h] |
| 200 | [Pank14] ¹⁶ [Zhu08] ²¹ [Neud06] ¹⁵ [Bali06] ¹⁶⁵ [Zett02] ²⁰ [Mart02] ¹⁴⁵ | 520 ± 20 | [Lade00] ⁸³ | 60 | (Hum22) ²⁹ (Bhat05) ⁸² [b] | 60 | [Nipo18] ³³ [h] |
| 200 | [Neud01] ¹⁴ [Habe94] ¹⁶⁶ [Pens93] ⁴⁰ | | [Rakn20] ¹⁷⁹ [Sull08] ¹⁷⁹ | 50 | [[min22] [Binat05] [h] | | [Kiiio14a] [ii] |
| | | 300 | [Neud06] ¹⁵ | 55 | [Levi01] [n] [iwat01] [n] | 56 | [Son06] ¹⁴⁴ [h] |
| 198 | [Kimo19] ¹⁵² [h] [Nipo18] ³³ [h] | 500 | [Huh06] ¹⁸⁰ [Neud01] ¹⁴ | 53 | [Gerh11] ¹⁸⁴ [h] | | |
| 107.0 | [Kimo14a] [ii] | | [Gao01]159 | 52.1 | [Buon12] ⁵⁹ [h] [Wang99] ¹⁶² [h] | 55 | [Dona18] ³¹ [h] |
| 197.9 | [Janz08] [1] | 202 | [Loph18]58 | 02.1 | [Pers99a] ¹⁰³ [h] [Greu9/] ¹⁴⁶ [h] [Bako9/] ⁶¹ [h] | | |
| 101 | [Bhat05] ⁸² [Zhao03] ¹⁶¹ | 295 | [Dona18] ¹⁵³ | 50 | [Sozz19] ¹⁷⁵ [Zhu08] ²¹ [h] [Zett02] ²⁰ [h] | 54 | [Zhu08] ²⁴ [h] |
| 191 | [Wang99] ¹⁶² [Pers98] ⁵¹ [Greu97] ¹⁴⁸ [Bako97] ⁸¹ [Made91] ¹⁵⁰ | | [Wije11] ¹⁵⁶ | 50 ± 5 | [Alba10] ³⁴ [h] [Schr06] ¹⁶⁸ [h] | 53 | [Zett02] ²⁰ [h] |
| | [bure),] [inne),] | 285 | [Zhu08] ²¹ | 50 ± 5 | [Ayal05] ⁸⁴ [h] [Ayal04] ⁶¹ [h] [Lade00] ⁸³ [h] | 55 | [Hand00] ²⁸ [h] |
| 100 | [Yosh18] ¹⁵⁴ [Megh18] ¹⁵⁵ | 205 | [Nego03] ¹⁵⁸ [Zett02] ²⁰ | 45 | [Wije11] ¹⁵⁶ [Neud06] ¹⁵ | 50 ± 5 | [A]ba10] ³⁴ [b] |
| 190 | [Wije11] ¹⁵⁶ [Nego04] ¹⁵⁷ | | | | [Neud01] ¹⁴ [Mick98] ¹⁸² [h] | 50 ± 5 | function full |
| | | 280 | [Kimo14a] ¹⁶⁴ | 44 42 | [Son06] ¹⁴⁴ [h] [Zhan10] ¹⁶⁰ | 45 | [Nego04a] ¹⁸⁸ |
| $150\pm5\text{+Ex}$ | [Hage73] ¹³⁷ | | | 33 | [Pank14] ¹⁶ [h] [Loma74] ¹⁸¹ | | |
| Δ | .1 | F | 3 | N | J | I |) |
| Γ | 11 | L | | 1 | 1 | 1 | |

142 [Son06]¹⁴⁴ [c]

125.5 [Janz08]¹⁶³ [c]

 120
 [Dona18]³¹ [c]

 110
 [Pern00]⁵³ [c]

 102
 [Levi01]¹¹ [c] [Iwat01]¹⁸⁵ [c]

126 [Kimo19]¹⁵² [c] [Kimo14a]¹⁶⁴ [c]

 $\frac{123.5}{124} \begin{array}{c} \text{[Ioff23]}^{147} \text{ [c]} \text{ [Fan14]}^{149} \text{ [c]} \\ \text{[Izz008]}^{187} \text{ [c]} \text{ [Made91]}^{150} \text{ [c]} \end{array}$

FIG. 5. Energy levels used in literature for each investigated dopant shown at the bottom. [c] marks cubic, [h] hexagonal and [e] effective values, i.e., a combination of hexagonal and cubic. Nodes with green background indicate a fundamental publication.



FIG. 6. Energy levels used in literature for acceptors and donors without closer specification of dopant element.



FIG. 7. Reference chain for n-type doping. Entries with green background show fundamental investigations, orange references we inferred based on the used data and blue investigation based not on 4H.

TABLE I. Parameters for the Pearson-Bardeen model (see Eq. (4)). Column N denotes how the factor N is interpreted: either as active dopants (dop), all dopants (tot), just the compensating ones (comp) or simply used in a fitting (fit). The site denotes besides hexagonal and cubic also a combined effective energy level (eff) and the deep level for Aluminium (deep). If left blank no information were stated in the paper.

| ref. | Ν | site | ΔE | α |
|-------------------------|------|-------|------------|----------------------------|
| | | | [meV] | [meV cm] |
| | | | | |
| Nitrogen | | | | |
| [Kaga04] ⁷⁰ | dop | hex | 70.9 | $3.38 	imes 10^{-5}$ |
| | | cubic | 123.7 | 4.65×10^{-5} |
| [Buon12] ⁵⁹ | tot | eff | 65 | $3.1 	imes 10^{-5}$ |
| [Hata13] ⁶⁰ | tot | eff | 105 | 4.26×10^{-5} |
| [Lech21] ¹⁴⁶ | tot | | 52.5 | 3.38×10^{-5} |
| | | | | |
| Phosphorous | S | | | |
| t.w. | fit | hex | 57 | $9.54	imes10^{-6}$ |
| | | cubic | 96 | 2.71×10^{-6} |
| | | | | |
| Aluminum | | | | |
| [Mats04] ⁵⁴ | dop | | 220 | $1.9 	imes 10^{-5}$ |
| [Pern05] ⁷¹ | dop | | 205 | $1.7 	imes 10^{-5}$ |
| [Acha08] ⁷² | dop | | 220 | 2.32×10^{-5} |
| [Koiz09] ¹⁰³ | dop | | 265 | $3.6 	imes 10^{-5}$ |
| [Buon12] ⁵⁹ | tot | eff | 210 | $3.1 	imes 10^{-5}$ |
| [Arvi17] ⁶⁹ | dop | | 230 ± 10 | $(2.8\pm0.3)\times10^{-5}$ |
| [Weis18] ⁷³ | dop | | 210 | 3×10^{-5} |
| [Kaji21] ⁷⁵ | comp | | 220 | $4.7 	imes 10^{-5}$ |
| [Lech21] ¹⁴⁶ | tot | | 230 | $1.8 	imes 10^{-5}$ |
| | | | | |
| Boron | | | | |
| [Lech21] ¹⁴⁶ | tot | | 345 | 3.1×10^{-5} |
| t.w. | fit | | 311 | 1.41×10^{-5} |

seldomly 6H data were used^{178,180}, whereat the values match those from 4H publications^{31,58,153}.

| TABLE II. Dopants and their respective cross sections with the charge carriers in the energetically closer |
|----------------------------------------------------------------------------------------------------------------|
| band (conduction or valence). Different temperature dependencies are indicated in the column T^{α} . We |
| found no data for Nitrogen. |

| ref. | site | T^{α} | ΔE | σ |
|-------------------------|-------|--------------|------------|-----------------------------|
| | | | [meV] | [cm ²] |
| | | | | |
| Nitrogen | | | | |
| [Kain99] ⁹² | cubic | T^0 | 77 | 7.92×10^{-15} |
| | | T^{-2} | 90 | 3.57×10^{-10} |
| Aluminum | | | | |
| [Kuzn95] ⁹³ | | T^{-3} | 229 | $8 	imes 10^{-13}$ |
| [Scha97] ⁵⁶ | | T^0 | 164–179 | $2.2 - 7.6 \times 10^{-13}$ |
| | | T^{-2} | 189–202 | $1.7 - 5.6 \times 10^{-12}$ |
| [Kain99] ⁹² | | T^0 | 189 | 2.58×10^{-13} |
| | | T^{-2} | 208 | 2.57×10^{-8} |
| [Resh05] ¹²⁹ | | T^0 | 185 | $1 	imes 10^{-14}$ |
| | | T^{-2} | 210 | $1 	imes 10^{-13}$ |
| [Belj10] ¹²⁸ | | T^0 | 200 | 1×10^{-12} |
| [Kawa15] ¹²⁷ | | T^0 | 190 | 1.4×10^{-13} |
| [Kato22] ¹³² | | T^0 | 120-170 | $1 - 100 	imes 10^{-17}$ |
| Boron | | | | |
| [Srid98a] ⁹¹ | | T^0 | 259–262 | - |
| | | T^{-2} | 284–295 | - |
| [Trof98] ⁴⁷ | | T^0 | 292 | $6 	imes 10^{-15}$ |
| | | T^{-2} | 314 | 5×10^{-14} |
| [Kain99] ⁹² | | T^0 | 312 | $2.1 	imes 10^{-14}$ |
| | | T^{-2} | 375 | 9.69×10^{-9} |
| [Zhan03] ¹³¹ | | T^0 | 230-280 | $2 - 30 \times 10^{-14}$ |

However, since the latter did not provide a reference for the picked values it is impossible to retrace where and how these values have been determined. Nevertheless we tried to create causality chains for n-type (see Fig. 7) p-type (see Fig. 8) values, whereat quite some values hat to be inferred due to missing information.

For n-type doping the values published by Ikeda, Matsunami, and Tanaka⁸⁰ are widely used



FIG. 8. Reference chain for p-type doping. Entries with green background show fundamental investigations, orange references we inferred based on the used data and blue investigation based not on 4H.

up until this day. Similarly, for p-type doping Götz *et al.*⁹⁸ provided for some time the values. However, recently the values by Ivanov, Henry, and Janzén¹³⁶, Ivanov, Magnusson, and Janzén¹⁴¹ are dominantly cited.

The most research has been clearly directed towards Aluminum. Overall, future research should be denoted to (i) gather additional data for Phosphorous and Boron and (ii) condense the already achieved values. For this purpose we added our own fittings based on the gathered data for cubic and hexagonal lattice site as well as for all values together (effective value).

REFERENCES

- ¹I. G. Atabaev, Kh. N. Juraev, and M. U. Hajiev, Journal of Spectroscopy **2018**, 1 (2018).
- ²J. M. Bluet, J. Pernot, J. Camassel, S. Contreras, J. L. Robert, J. F. Michaud, and T. Billon, Journal of Applied Physics **88**, 1971 (2000).
- ³T. Dalibor and M. Schulz, eds., *Numerical Data and Functional Relationships in Science and Technology. Subvol. A2: Gruppe 3: Kristall- Und Festkörperphysik = Group 3: @Crystal and Solid State Physics Vol. 41, Semiconductors Impurities and Defects in Group IV Elements, IV-IV and III-V Compounds. Part Beta: Group IV-IV and III-V Compounds / Ed. by M. Schulz; Authors: T. Dalibor, Vol. 41 (Springer, Berlin Heidelberg, 2003).*
- ⁴G. Dhanaraj, K. Byrappa, V. Prasad, and M. Dudley, eds., *Springer Handbook of Crystal Growth* (Springer Berlin Heidelberg, Berlin, Heidelberg, 2010).
- ⁵Z. C. Feng and J. H. Zhao, eds., *Silicon Carbide: Materials, Processing, and Devices*, Optoelectronic Properties of Semiconductors and Superlattices No. v. 20 (Taylor & Francis, New York, 2004).
- ⁶G. L. Harris and Inspec, eds., *Properties of Silicon Carbide*, EMIS Datareviews Series No. 13 (INSPEC, the Inst. of Electrical Engineers, London, 1995).
- ⁷V. Heera, D. Panknin, and W. Skorupa, Applied Surface Science **184**, 307 (2001).
- ⁸T. Kimoto, Japanese Journal of Applied Physics **54**, 040103 (2015).
- ⁹P. Kwasnicki, *Evaluation of Doping in 4H-SiC by Optical Spectroscopies*, Ph.D. thesis, UNI-VERSITE MONTPELLIER II (2014).
- ¹⁰A. A. Lebedev, Semiconductors **33**, 107 (1999).
- ¹¹M. E. Levinshteĭn, S. L. Rumyantsev, and M. Shur, eds., *Properties of Advanced Semiconductor Materials: GaN, AlN, InN, BN, SiC, SiGe* (Wiley, New York, 2001).
- ¹²J. Lutz, H. Schlangenotto, U. Scheuermann, and R. De Doncker, *Semiconductor Power Devices: Physics, Characteristics, Reliability* (Springer Berlin Heidelberg, Berlin, Heidelberg, 2011).
- ¹³J. Lutz, U. Scheuermann, H. Schlangenotto, and R. De Doncker, "Power Semiconductor Devices—Key Components for Efficient Electrical Energy Conversion Systems," in *Semiconductor Power Devices* (Springer International Publishing, Cham, 2018) pp. 1–20.
- ¹⁴P. Neudeck, in *Encyclopedia of Materials: Science and Technology* (Elsevier, 2001) pp. 8508– 8519.

¹⁵P. G. Neudeck (2006).

- ¹⁶Electroluminescence, softcover reprint of the original 1st ed. 1977 ed. (Springer Berlin, Berlin, 2014).
- ¹⁷G. Pensl, F. Ciobanu, T. Frank, M. Krieger, S. Reshanov, F. Schmid, and M. Weidner, International Journal of High Speed Electronics and Systems **15**, 705 (2005).
- ¹⁸C. Persson and A. Ferreira Da Silva, in *Optoelectronic Devices: III Nitrides* (Elsevier, 2005) pp. 479–559.
- ¹⁹R. Wang, Y. Huang, D. Yang, and X. Pi, Applied Physics Letters **122**, 180501 (2023).
- ²⁰C.-M. Zetterling, ed., *Process Technology for Silicon Carbide Devices*, EMIS Processing Series
 No. 2 (Institution of Electrical Engineers, London, 2002).
- ²¹X. Zhu, *ALTERNATIVE GROWTH AND INTERFACE PASSIVATION TECHNIQUES FOR SiO2 ON 4H-SiC*, Ph.D. thesis, Auburn University (2008).
- ²²M. Miyata, Y. Higashiguchi, and Y. Hayafuji, Journal of Applied Physics **104**, 123702 (2008).
- ²³J. Senzaki, K. Fukuda, Y. Ishida, Y. Tanaka, H. Tanoue, N. Kobayashi, T. Tanaka, and K. Arai, MRS Proceedings 622, T6.7.1 (2000).
- ²⁴T. Troffer, G. Pensl, A. Schöner, A. Henry, C. Hallin, Kordina, and E. Janzén, Materials Science Forum 264–268 (1998), 10.4028/www.scientific.net/MSF.264-268.557.
- ²⁵M. Krieger, M. Rühl, T. Sledziewski, G. Ellrott, T. Palm, H. B. Weber, and M. Bockstedte, Materials Science Forum 858, 301 (2016).
- ²⁶Y. Huang, R. Wang, Y. Qian, Y. Zhang, D. Yang, and X. Pi, Chinese Physics B **31**, 046104 (2022).
- ²⁷T. Dalibor, G. Pensl, H. Matsunami, T. Kimoto, W. J. Choyke, A. Schöner, and N. Nordell, physica status solidi (a) 162, 199 (1997).
- ²⁸E. M. Handy, M. V. Rao, O. W. Holland, K. A. Jones, M. A. Derenge, and N. Papanicolaou, Journal of Applied Physics 88, 5630 (2000).
- ²⁹Y. Huang, R. Wang, Y. Zhang, D. Yang, and X. Pi, Chinese Physics B **31**, 056108 (2022).
- ³⁰G. Xiao, J. Lee, J. Liou, and A. Ortiz-Conde, Microelectronics Reliability **39**, 1299 (1999).
- ³¹N. Donato and F. Udrea, IEEE Transactions on Electron Devices **65**, 4469 (2018).
- ³²R. . Scaburri, (2011), 10.6092/UNIBO/AMSDOTTORATO/3924.
- ³³R. Nipoti, H. M. Ayedh, and B. G. Svensson, Materials Science in Semiconductor Processing 78, 13 (2018).
- ³⁴L. F. Albanese, Characterization, Modeling and Simulation of 4H-SiC Power Diodes, Ph.D.

thesis, UniversitàdegliStudidiSalerno (2010).

- ³⁵C. Darmody and N. Goldsman, Journal of Applied Physics **126**, 145701 (2019).
- ³⁶F. Bechstedt, J. Furthmüller, U. Grossner, and C. Raffy, in *Silicon Carbide*, edited by W. J. Choyke, H. Matsunami, and G. Pensl (Springer Berlin Heidelberg, Berlin, Heidelberg, 2004) pp. 3–25.
- ³⁷N. T. Son, Mt. Wagner, C. G. Hemmingsson, L. Storasta, B. Magnusson, W. M. Chen, S. Greulich-Weber, J.-M. Spaeth, and E. Janzén, in *Silicon Carbide*, edited by W. J. Choyke, H. Matsunami, and G. Pensl (Springer Berlin Heidelberg, Berlin, Heidelberg, 2004) pp. 461–492.
- ³⁸M. Laube, F. Schmid, K. Semmelroth, G. Pensl, R. P. Devaty, W. J. Choyke, G. Wagner, and M. Maier, in *Silicon Carbide*, edited by W. J. Choyke, H. Matsunami, and G. Pensl (Springer Berlin Heidelberg, Berlin, Heidelberg, 2004) pp. 493–515.
- ³⁹V. J. B. Torres, I. Capan, and J. Coutinho, Physical Review B **106**, 224112 (2022).
- ⁴⁰G. Pensl and W. Choyke, Physica B: Condensed Matter **185**, 264 (1993).
- ⁴¹Q. Chen, W. He, C. Cheng, and Y. Xue, Journal of Physics: Conference Series **1649**, 012048 (2020).
- ⁴²S. M. Sze and K. K. Ng, *Physics of Semiconductor Devices*, 3rd ed. (Wiley-Interscience, Hoboken, N.J, 2007).
- ⁴³V. Uhnevionak, *Simulation and Modeling of Silicon-Carbide Devices*, Ph.D. thesis, Friedrich-Alexander-Universität (2015).
- ⁴⁴H. Habib, N. G. Wright, and A. B. Horsfall, Advanced Materials Research **413**, 229 (2011).
- ⁴⁵J. Blakemore, *Semiconductor Statistics* (Elsevier, 1962).
- ⁴⁶F. Schmid, M. Krieger, M. Laube, G. Pensl, and G. Wagner, in *Silicon Carbide*, edited by W. J. Choyke, H. Matsunami, and G. Pensl (Springer Berlin Heidelberg, Berlin, Heidelberg, 2004) pp. 517–536.
- ⁴⁷T. Troffer, *Elektrische Und Optische Charakterisierung Bauelementrelevanter Dotierstoffe in Siliciumkarbid*, Ph.D. thesis, FriedrichAlexander-Universität (1998).
- ⁴⁸M. Laube, F. Schmid, G. Pensl, G. Wagner, M. Linnarsson, and M. Maier, Journal of Applied Physics **92**, 549 (2002).
- ⁴⁹S. Balachandran, T. P. Chow, and A. K. Agarwal, Materials Science Forum **483–485**, 909 (2005).
- ⁵⁰M. Nawaz, Microelectronics Journal **41**, 801 (2010).

- ⁵¹C. Persson and U. Lindefelt, Materials Science Forum 264–268, 275 (1998).
- ⁵²Z. Lv, J. Li, L. Dong, and J. Zang, in 2023 International Conference on Telecommunications, Electronics and Informatics (ICTEI) (IEEE, Lisbon, Portugal, 2023) pp. 269–273.
- ⁵³J. Pernot, S. Contreras, J. Camassel, J. L. Robert, W. Zawadzki, E. Neyret, and L. Di Cioccio, Applied Physics Letters 77, 4359 (2000).
- ⁵⁴H. Matsuura, M. Komeda, S. Kagamihara, H. Iwata, R. Ishihara, T. Hatakeyama, T. Watanabe, K. Kojima, T. Shinohe, and K. Arai, Journal of Applied Physics 96, 2708 (2004).
- ⁵⁵H. Matsuura, Materials Science Forum **389–393**, 679 (2002).
- ⁵⁶M. Schadt, *Transporteigenschaften von Elektronen Und Löchern in Siliciumkarbid*, Ph.D. thesis, FriedrichAlexander-Universität (1997).
- ⁵⁷J. Pernot, W. Zawadzki, S. Contreras, J. L. Robert, E. Neyret, and L. Di Cioccio, Journal of Applied Physics **90**, 1869 (2001).
- ⁵⁸N. Lophitis, A. Arvanitopoulos, S. Perkins, and M. Antoniou, in *Disruptive Wide Bandgap Semiconductors, Related Technologies, and Their Applications*, edited by Y. K. Sharma (In-Tech, 2018).
- ⁵⁹B. Buono, *Simulation and Characterization of Silicon Carbide Power Bipolar Junction Transistors*, Ph.D. thesis, KTH Royal Institute of Technology (2012).
- ⁶⁰T. Hatakeyama, K. Fukuda, and H. Okumura, IEEE Transactions on Electron Devices **60**, 613 (2013).
- ⁶¹T. Ayalew, *SiC Semiconductor Devices Technology, Modeling, and Simulation*, Ph.D. thesis, TU Wien (2004).
- ⁶²S. K. Lee, *Processing and Characterization of Silicon Carbide (6H-SiC and 4H-SiC) Contacts for High Power and h...* (Mikroelektronik och informationsteknik, Kista, 2002).
- ⁶³K. Zeghdar, L. Dehimi, F. Pezzimenti, S. Rao, and F. G. Della Corte, Japanese Journal of Applied Physics **58**, 014002 (2019).
- ⁶⁴K. Zeghdar, L. Dehimi, F. Pezzimenti, M. L. Megherbi, and F. G. Della Corte, Journal of Electronic Materials **49**, 1322 (2020).
- ⁶⁵M. Ruff, H. Mitlehner, and R. Helbig, IEEE Transactions on Electron Devices **41**, 1040 (1994).
- ⁶⁶T. Troffer, M. Schadt, T. Frank, H. Itoh, G. Pensl, J. Heindl, H. P. Strunk, and M. Maier, physica status solidi (a) **162**, 277 (1997).
- ⁶⁷C. M. Zetterling, M. Östling, C. I. Harris, N. Nordell, K. Wongchotigul, and M. G. Spencer, Materials Science Forum 264–268, 877 (1998).

- ⁶⁸G. L. Pearson and J. Bardeen, Physical Review 75, 865 (1949).
- ⁶⁹I.-R. Arvinte, *Investigation of Dopant Incorporation in Silicon Carbide Epilayers Grown by Chemical Vapor Deposition*, Ph.D. thesis, Universite Cote d'Azur (2017).
- ⁷⁰S. Kagamihara, H. Matsuura, T. Hatakeyama, T. Watanabe, M. Kushibe, T. Shinohe, and K. Arai, Journal of Applied Physics 96, 5601 (2004).
- ⁷¹J. Pernot, S. Contreras, and J. Camassel, Journal of Applied Physics **98**, 023706 (2005).
- ⁷²P. Achatz, J. Pernot, C. Marcenat, J. Kacmarcik, G. Ferro, and E. Bustarret, Applied Physics Letters **92**, 072103 (2008).
- ⁷³J. Weiße, M. Hauck, T. Sledziewski, M. Tschiesche, M. Krieger, A. J. Bauer, H. Mitlehner, L. Frey, and T. Erlbacher, Materials Science Forum 924, 184 (2018).
- ⁷⁴H. Tanaka, S. Asada, T. Kimoto, and J. Suda, Journal of Applied Physics **123**, 245704 (2018).
- ⁷⁵Y. Kajikawa, Journal of Electronic Materials **50**, 1247 (2021).
- ⁷⁶M. Rambach, A. J. Bauer, and H. Ryssel, physica status solidi (b) **245**, 1315 (2008).
- ⁷⁷R. Scaburri, A. Desalvo, and R. Nipoti, Materials Science Forum **679–680**, 397 (2011).
- ⁷⁸P. P. Altermatt, A. Schenk, and G. Heiser, Journal of Applied Physics **100**, 113714 (2006).
- ⁷⁹P. P. Altermatt, A. Schenk, B. Schmithüsen, and G. Heiser, Journal of Applied Physics **100**, 113715 (2006).
- ⁸⁰M. Ikeda, H. Matsunami, and T. Tanaka, Physical Review B 22, 2842 (1980).
- ⁸¹M. Bakowski, U. Gustafsson, and U. Lindefelt, physica status solidi (a) 162, 421 (1997).
- ⁸²P. Bhatnagar, A. B. Horsfall, N. G. Wright, C. M. Johnson, K. V. Vassilevski, and A. G. O'Neill, Solid-State Electronics **49**, 453 (2005).
- ⁸³M. Lades, *Modeling and Simulation of Wide Bandgap Semiconductor Devices: 4H/6H-SiC*,
 Ph.D. thesis, Technische Universität München (2000).
- ⁸⁴T. Ayalew, T. Grasser, H. Kosina, and S. Selberherr, Materials Science Forum **483–485**, 845 (2005).
- ⁸⁵I. D. Booker, *Carrier Lifetime Relevant Deep Levels in SiC*, Linköping Studies in Science and Technology. Dissertations, Vol. 1714 (Linköping University Electronic Press, Linköping, 2015).
- ⁸⁶P. T. Landsberg, physica status solidi (b) **41**, 457 (1970).
- ⁸⁷B. K. Ridley, Journal of Physics C: Solid State Physics **11**, 2323 (1978).
- ⁸⁸M. Lades, W. Kaindl, N. Kaminski, E. Niemann, and G. Wachutka, IEEE Transactions on Electron Devices **46**, 598 (1999).

⁸⁹M. Lax, Physical Review **119**, 1502 (1960).

- ⁹⁰V. N. Abakumov, V. I. Perel, and I. N. Yassievich, *Nonradiative Recombination in Semiconductors*, Modern Problems in Condensed Matter Sciences No. v. 33 (North-Holland ; Sole distributors for the USA and Canada, Elsevier Science Pub. Co, Amsterdam ; New York : New York, NY, USA, 1991).
- ⁹¹S. G. Sridhara, L. L. Clemen, R. P. Devaty, W. J. Choyke, D. J. Larkin, H. S. Kong, T. Troffer, and G. Pensl, Journal of Applied Physics **83**, 7909 (1998).
- ⁹²W. Kaindl, M. Lades, N. Kaminski, E. Niemann, and G. Wachutka, Journal of Electronic Materials 28, 154 (1999).
- ⁹³N. Kuznetsov and A. Zubrilov, Materials Science and Engineering: B 29, 181 (1995).
- ⁹⁴S. Asada, T. Okuda, T. Kimoto, and J. Suda, Applied Physics Express 9, 041301 (2016).
- ⁹⁵M. A. Capano, J. A. Cooper, M. R. Melloch, A. Saxler, and W. C. Mitchel, Journal of Applied Physics 87, 8773 (2000).
- ⁹⁶W. Choyke and G. Pensl, MRS Bulletin **22**, 25 (1997).
- ⁹⁷S. Contreras, L. Konczewicz, P. Kwasnicki, R. Arvinte, H. Peyre, T. Chassagne, M. Zielinski, M. Kayambaki, S. Juillaguet, and K. Zekentes, Materials Science Forum 858, 249 (2016).
- ⁹⁸W. Götz, A. Schöner, G. Pensl, W. Suttrop, W. J. Choyke, R. Stein, and S. Leibenzeder, Journal of Applied Physics **73**, 3332 (1993).
- ⁹⁹C. Hitchcock, R. Ghandi, P. Deeb, S. Kennerly, M. Torky, and T. P. Chow, Materials Science Forum **1062**, 422 (2022).
- ¹⁰⁰H. Itoh, T. Troffer, and G. Pensl, Materials Science Forum **264–268**, 685 (1998).
- ¹⁰¹L. Kasamakova-Kolaklieva, L. Storasta, I. G. Ivanov, B. Magnusson, S. Contreras, C. Consejo,
 J. Pernot, M. Zielinski, and E. Janzén, Materials Science Forum 457–460, 677 (2004).
- ¹⁰²T. Kimoto, A. Itoh, H. Matsunami, S. Sridhara, L. L. Clemen, R. P. Devaty, W. J. Choyke, T. Dalibor, C. Peppermüller, and G. Pensl, Applied Physics Letters 67, 2833 (1995).
- ¹⁰³A. Koizumi, J. Suda, and T. Kimoto, Journal of Applied Physics **106**, 013716 (2009).
- ¹⁰⁴D. J. Lichtenwalner, J. H. Park, S. Rogers, H. Dixit, A. Scholtze, S. Bubel, and S. H. Ryu, Materials Science Forum **1089**, 3 (2023).
- ¹⁰⁵G. Lomakina and Y. A. Vodakov, **15**, 83 (1973).
- ¹⁰⁶H. Matsuura, T. K. Tsunenobu Kimoto, and H. M. Hiroyuki Matsunami, Japanese Journal of Applied Physics **38**, 4013 (1999).
- ¹⁰⁷R. Nipoti, R. Scaburri, A. Hallén, and A. Parisini, Journal of Materials Research 28, 17 (2013).

- ¹⁰⁸M. Obernhofer, M. Krieger, F. Schmid, H. B. Weber, G. Pensl, and A. Schöner, Materials Science Forum 556–557, 343 (2007).
- ¹⁰⁹A. Parisini and R. Nipoti, Journal of Applied Physics **114**, 243703 (2013).
- ¹¹⁰G. Pensl, F. Schmid, F. Ciobanu, M. Laube, S. A. Reshanov, N. Schulze, K. Semmelroth, A. Schöner, G. Wagner, and H. Nagasawa, Materials Science Forum 433–436, 365 (2003).
- ¹¹¹M. Rambach, L. Frey, A. J. Bauer, and H. Ryssel, Materials Science Forum **527–529**, 827 (2006).
- ¹¹²M. V. Rao, J. B. Tucker, M. C. Ridgway, O. W. Holland, N. Papanicolaou, and J. Mittereder, Journal of Applied Physics 86, 752 (1999).
- ¹¹³S. Rao, T. P. Chow, and I. Bhat, Materials Science Forum **527–529**, 597 (2006).
- ¹¹⁴G. Rutsch, R. P. Devaty, W. J. Choyke, D. W. Langer, and L. B. Rowland, Journal of Applied Physics **84**, 2062 (1998).
- ¹¹⁵N. S. Saks, A. K. Agarwal, S.-H. Ryu, and J. W. Palmour, Journal of Applied Physics **90**, 2796 (2001).
- ¹¹⁶N. S. Saks, A. V. Suvorov, and D. C. Capell, Applied Physics Letters 84, 5195 (2004).
- ¹¹⁷F. Schmid, M. Laube, G. Pensl, G. Wagner, and M. Maier, Journal of Applied Physics 91, 9182 (2002).
- ¹¹⁸A. Schöner, S. Karlsson, T. Schmitt, N. Nordell, M. Linnarsson, and K. Rottner, Materials Science and Engineering: B 61–62, 389 (1999).
- ¹¹⁹Y. Tanaka, N. Kobayashi, H. Okumura, R. Suzuki, T. Ohdaira, M. Hasegawa, M. Ogura, S. Yoshida, and H. Tanoue, Materials Science Forum 338–342, 909 (2000).
- ¹²⁰P. Terziyska, C. Blanc, J. Pernot, H. Peyre, S. Contreras, G. Bastide, J. L. Robert, J. Camassel,
 E. Morvan, C. Dua, and C. C. Brylinski, physica status solidi (a) 195, 243 (2003).
- ¹²¹G. Wagner, W. Leitenberger, K. Irmscher, F. Schmid, M. Laube, and G. Pensl, Materials Science Forum 389–393, 207 (2002).
- ¹²²R. Wang, I. B. Bhat, and T. P. Chow, Journal of Applied Physics **92**, 7587 (2002).
- ¹²³S. Y. Ji, K. Kojima, Y. Ishida, H. Tsuchida, S. Yoshida, and H. Okumura, Materials Science Forum 740–742, 181 (2013).
- ¹²⁴H. Matsuura, K. Aso, S. Kagamihara, H. Iwata, T. Ishida, and K. Nishikawa, Applied Physics Letters 83, 4981 (2003).
- ¹²⁵A. O. Evwaraye, S. R. Smith, and W. C. Mitchel, Journal of Applied Physics **79**, 7726 (1996).
- ¹²⁶S. Smith, A. Evwaraye, and W. Mitchel, MRS Proceedings **510**, 193 (1998).

- ¹²⁷K. Kawahara, H. Watanabe, N. Miura, S. Nakata, and S. Yamakawa, Materials Science Forum 821–823, 403 (2015).
- ¹²⁸S. Beljakowa, S. A. Reshanov, B. Zippelius, M. Krieger, G. Pensl, K. Danno, T. Kimoto, S. Onoda, T. Ohshima, F. Yan, R. P. Devaty, and W. J. Choyke, Materials Science Forum 645–648, 427 (2010).
- ¹²⁹S. Reshanov, *Device-Relevant Defect Centers and Minority Carrier Lifetime in 3C-, 4H- and 6H-SiC*, Ph.D. thesis, Erlangen-Nürnberg, Germany (2005).
- ¹³⁰C. Kisielowski, K. Maier, J. Schneider, and V. Oding, Materials Science Forum 83–87, 1171 (1992).
- ¹³¹J. Zhang, L. Storasta, J. P. Bergman, N. T. Son, and E. Janzén, Journal of Applied Physics 93, 4708 (2003).
- ¹³²M. Kato, J. Di, Y. Ohkouchi, T. Mizuno, M. Ichimura, and K. Kojima, Materials Today Communications **31**, 103648 (2022).
- ¹³³C. Q. Chen, J. Zeman, F. Engelbrecht, C. Peppermüller, R. Helbig, Z. H. Chen, and G. Martinez, Journal of Applied Physics 87, 3800 (2000).
- ¹³⁴R. P. Devaty and W. J. Choyke, physica status solidi (a) **162**, 5 (1997).
- ¹³⁵I. G. Ivanov, B. Magnusson, and E. Janzén, Physical Review B 67, 165211 (2003).
- ¹³⁶I. G. Ivanov, A. Henry, and E. Janzén, Physical Review B **71**, 241201 (2005).
- ¹³⁷S. Hagen, A. Van Kemenade, and J. Van Der Does De Bye, Journal of Luminescence 8, 18 (1973).
- ¹³⁸H. Matsunami, A. Suzuki, and T. Tanaka, in *In: Silicon Carbide-1973; Proceedings of the Third International Conference* (1974) pp. 618–625.
- ¹³⁹A. Suzuki, H. Matsunami, and T. Tanaka, Japanese Journal of Applied Physics **12**, 1083 (1973).
- ¹⁴⁰A. Suzuki, H. Matsunami, and T. Tanaka, Journal of The Electrochemical Society **124**, 241 (1977).
- ¹⁴¹I. G. Ivanov, B. Magnusson, and E. Janzén, Physical Review B 67, 165212 (2003).
- ¹⁴²L. Lu, H. Zhang, X. Wu, J. Shi, and Y.-Y. Sun, Chinese Physics B **30**, 096806 (2021).
- ¹⁴³A.-B. Chen and P. Srichaikul, physica status solidi (b) **202**, 81 (1997).
- ¹⁴⁴N. T. Son, A. Henry, J. Isoya, M. Katagiri, T. Umeda, A. Gali, and E. Janzén, Physical Review B 73, 075201 (2006).
- ¹⁴⁵A. Martinez, U. Lindefelt, M. Hjelm, and H.-E. Nilsson, Journal of Applied Physics **91**, 1359 (2002).

- ¹⁴⁶B. Lechner, *Behaviour of 4H-SiC Power Semiconductor Devices under Extreme Operating Conditions*, Ph.D. thesis, Technische Universität München (2021).
- ¹⁴⁷I. Institute, "Silicon Carbide," http://www.ioffe.ru/SVA/NSM/Semicond/SiC/index.html.
- ¹⁴⁸S. Greulich-Weber, physica status solidi (a) **162**, 95 (1997).
- ¹⁴⁹J. Fan and P. K. Chu, "General Properties of Bulk SiC," in *Silicon Carbide Nanostructures* (Springer International Publishing, Cham, 2014) pp. 7–114.
- ¹⁵⁰O. Madelung and R. Poerschke, eds., *Semiconductors: Group IV Elements and III-V Compounds*, Data in Science and Technology (Springer Berlin Heidelberg, Berlin, Heidelberg, 1991).
- ¹⁵¹M. Bockstedte, A. Mattausch, and O. Pankratov, Applied Physics Letters 85, 58 (2004).
- ¹⁵²T. Kimoto, in *Wide Bandgap Semiconductor Power Devices* (Elsevier, 2019) pp. 21-42.
- ¹⁵³A. Arvanitopoulos, N. Lophitis, S. Perkins, K. N. Gyftakis, M. Belanche Guadas, and M. Antoniou, in 2017 IEEE 11th International Symposium on Diagnostics for Electrical Machines, Power Electronics and Drives (SDEMPED) (IEEE, Tinos, Greece, 2017) pp. 565–571.
- ¹⁵⁴H. Yoshioka and K. Hirata, AIP Advances 8, 045217 (2018).
- ¹⁵⁵M. L. Megherbi, F. Pezzimenti, L. Dehimi, M. A. Saadoune, and F. G. Della Corte, IEEE Transactions on Electron Devices **65**, 3371 (2018).
- ¹⁵⁶M. B. Wijesundara and R. Azevedo, *Silicon Carbide Microsystems for Harsh Environments*, MEMS Reference Shelf, Vol. 22 (Springer New York, New York, NY, 2011).
- ¹⁵⁷Y. Negoro, T. Kimoto, H. Matsunami, F. Schmid, and G. Pensl, Journal of Applied Physics **96**, 4916 (2004).
- ¹⁵⁸Y. Negoro, T. Kimoto, and H. Matsunami, Electronics and Communications in Japan (Part II: Electronics) 86, 44 (2003).
- ¹⁵⁹Y. Gao, S. I. Soloviev, T. S. Sudarshan, and C.-C. Tin, Journal of Applied Physics **90**, 5647 (2001).
- ¹⁶⁰Y.-R. Zhang, B. Zhang, Z.-J. Li, and X.-C. Deng, Chinese Physics B **19**, 067102 (2010).
- ¹⁶¹J. Zhao, X. Li, K. Tone, P. Alexandrov, M. Pan, and M. Weiner, Solid-State Electronics 47, 377 (2003).
- ¹⁶²J. Wang and B. W. Williams, Semiconductor Science and Technology 14, 1088 (1999).
- ¹⁶³E. Janzén, A. Gali, A. Henry, I. G. Ivanov, B. Magnusson, and N. T. Son, in *Defects in Micro-electronic Materials and Devices* (2008) pp. 615–669.
- ¹⁶⁴T. Kimoto and J. A. Cooper, Fundamentals of Silicon Carbide Technology: Growth, Charac-

terization, Devices, and Applications, 1st ed. (Wiley, 2014).

- ¹⁶⁵B. J. Baliga, *Silicon Carbide Power Devices* (WORLD SCIENTIFIC, 2006).
- ¹⁶⁶Ch. Haberstroh, R. Helbig, and R. A. Stein, Journal of Applied Physics 76, 509 (1994).
- ¹⁶⁷K. Tian, J. Xia, K. Elgammal, A. Schöner, W. Kaplan, R. Karhu, J. Ul-Hassan, and A. Hallén, Materials Science in Semiconductor Processing **115**, 105097 (2020).
- ¹⁶⁸D. Schröder, *Leistungselektronische Bauelemente* (Springer Berlin Heidelberg, Berlin, Heidelberg, 2006).
- ¹⁶⁹M. Usman, B. Buono, and A. Hallen, IEEE Transactions on Electron Devices **59**, 3371 (2012).
- ¹⁷⁰B. Buono, R. Ghandi, M. Domeij, B. G. Malm, C.-M. Zetterling, and M. Ostling, IEEE Transactions on Electron Devices **57**, 704 (2010).
- ¹⁷¹R. Trew, Proceedings of the IEEE **90**, 1032 (2002).
- ¹⁷²Y. Huang, R. Wang, Y. Zhang, D. Yang, and X. Pi, Journal of Applied Physics **131**, 185703 (2022).
- ¹⁷³A. K. Tiwari, M. Antoniou, N. Lophitis, S. Perkin, T. Trajkovic, and F. Udrea, IEEE Transactions on Electron Devices **66**, 3066 (2019).
- ¹⁷⁴A. K. Tiwari, F. Udrea, N. Lophitis, and M. Antoniou, in 2019 31st International Symposium on Power Semiconductor Devices and ICs (ISPSD) (IEEE, Shanghai, China, 2019) pp. 175–178.
- ¹⁷⁵G. Sozzi, M. Puzzanghera, R. Menozzi, and R. Nipoti, IEEE Transactions on Electron Devices66, 3028 (2019).
- ¹⁷⁶D. Johannesson, M. Nawaz, and H. P. Nee, Materials Science Forum **963**, 670 (2019).
- ¹⁷⁷H. K. Henisch and R. Roy, *Silicon Carbide—1968: Proceedings of the International Conference on Silicon Carbide, University Park, Pennsylvania, October 20-23, 1968* (Elsevier, 2013).
- ¹⁷⁸S. Rakheja, L. Huang, S. Hau-Riege, S. E. Harrison, L. F. Voss, and A. M. Conway, IEEE Journal of the Electron Devices Society **8**, 1118 (2020).
- ¹⁷⁹J. Sullivan and J. Stanley, IEEE Transactions on Plasma Science **36**, 2528 (2008).
- ¹⁸⁰S. W. Huh, J. J. Sumakeris, A. Polyakov, M. Skowronski, P. B. Klein, B. Shanabrook, and M. J. O'Loughlin, Materials Science Forum **527–529**, 493 (2006).
- ¹⁸¹G. Lomakina, in In: Silicon Carbide-1973; Proceedings of the Third International Conference (1974) pp. 520–526.
- ¹⁸²R. Mickevičius and J. H. Zhao, Journal of Applied Physics 83, 3161 (1998).
- ¹⁸³C. Persson, U. Lindefelt, and B. E. Sernelius, Physical Review B 60, 16479 (1999).
- ¹⁸⁴Properties and Applications of Silicon Carbide (IntechOpen, Erscheinungsort nicht ermittelbar,

2011).

- ¹⁸⁵H. Iwata and K. M. Itoh, Journal of Applied Physics 89, 6228 (2001).
- ¹⁸⁶A. Yang, K. Murata, T. Miyazawa, T. Tawara, and H. Tsuchida, Journal of Applied Physics 126, 055103 (2019).
- ¹⁸⁷G. Izzo, G. Litrico, L. Calcagno, G. Foti, and F. La Via, Journal of Applied Physics **104**, 093711 (2008).
- ¹⁸⁸Y. Negoro, K. Katsumoto, T. Kimoto, and H. Matsunami, Journal of Applied Physics **96**, 224 (2004).
- ¹⁸⁹F. Pezzimenti, IEEE Transactions on Electron Devices **60**, 1404 (2013).
- ¹⁹⁰S. Bellone, F. G. Della Corte, L. F. Albanese, and F. Pezzimenti, IEEE Transactions on Power Electronics **26**, 2835 (2011).
- ¹⁹¹F. Pezzimenti, L. F. Albanese, S. Bellone, and F. G. D. Corte, in 2009 IEEE Bipolar/BiCMOS Circuits and Technology Meeting (IEEE, Capri, Italy, 2009) pp. 214–217.
- ¹⁹²H. Liu, J. Wang, S. Liang, H. Yu, and W. Deng, Semiconductor Science and Technology 36, 025009 (2021).
- ¹⁹³M. L. Megherbi, L. Dehimi, W. terghini, F. Pezzimenti, and F. G. Della Corte, Courrier du Savoir 19, 71 (2015).
- ¹⁹⁴X. Li, Y. Luo, L. Fursin, J. Zhao, M. Pan, P. Alexandrov, and M. Weiner, Solid-State Electronics
 47, 233 (2003).
- ¹⁹⁵S. Rao, E. D. Mallemace, and F. G. Della Corte, Electronics **11**, 1839 (2022).
- ¹⁹⁶S. J. Bader, H. Lee, R. Chaudhuri, S. Huang, A. Hickman, A. Molnar, H. G. Xing, D. Jena, H. W. Then, N. Chowdhury, and T. Palacios, IEEE Transactions on Electron Devices 67, 4010 (2020).
- ¹⁹⁷S. J. Pearton, X. Xia, F. Ren, M. A. J. Rasel, S. Stepanoff, N. Al-Mamun, A. Haque, and D. E. Wolfe, Journal of Vacuum Science & Technology B **41**, 030802 (2023).
- ¹⁹⁸M. Roschke, F. Schwierz, G. Paasch, and D. Schipanski, Materials Science Forum **264–268**, 965 (1998).
- ¹⁹⁹G. Pensl, ed., Silicon Carbide, III-nitrides and Related Materials: Proceedings of the 7th International Conference on Silicon Carbide, III-Nitrides and Related Materials, Stockholm, Sweden, September 1997, Materials Science Forum No. 264/268 (1998).
- ²⁰⁰K. Adachi, Simulation and Modelling of Power Devices Based on 4H Silicon Carbide, Ph.D. thesis, University of Newcastle (2003).

- ²⁰¹T. Tamaki, G. G. Walden, Y. Sui, and J. A. Cooper, IEEE Transactions on Electron Devices **55**, 1920 (2008).
- ²⁰²K. G. Menon, A. Nakajima, L. Ngwendson, and E. M. Sankara Narayanan, IEEE Electron Device Letters **32**, 1272 (2011).
- ²⁰³S. I. Maximenko, AIP Advances **13**, 105021 (2023).
- ²⁰⁴S. R. Smith, A. O. Evwaraye, W. C. Mitchel, and M. A. Capano, Journal of Electronic Materials28, 190 (1999).
- ²⁰⁵A. Gali, P. Deák, R. P. Devaty, and W. J. Choyke, Physical Review B **60**, 10620 (1999).